

Microsoft PowerPoint® Presentation Graphics for
EE 313: Basic Electrical Engineering I

Prepared by Brian Manhire, Ph.D.
 Professor of Electrical Engineering



*Stocker Center, home of Ohio University's
 Russ College of Engineering & Technology*

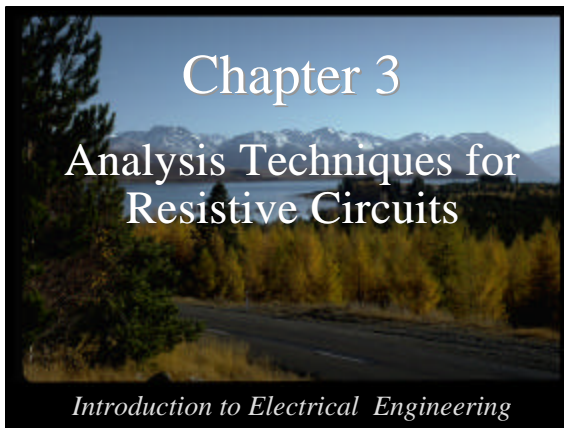
Microsoft PowerPoint® Presentation Graphics
 © Copyright 1998 Brian Manhire

For Part 1 of

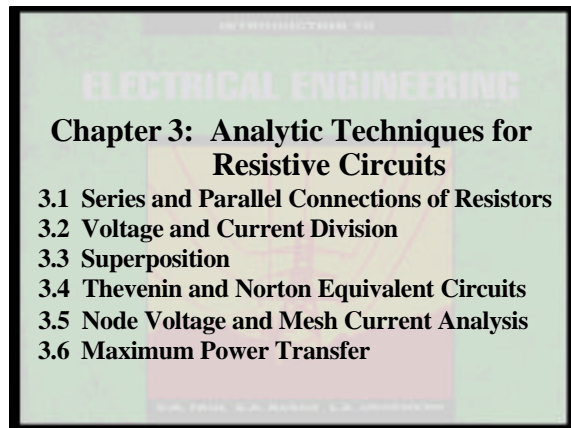
**Introduction to Electrical
 Engineering, 2/e**

by **C.R. Paul, S.A. Nasar
 and L.E. Unnewehr**

© 1992, McGraw-Hill, Inc.

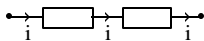


Introduction to Electrical Engineering



3.1 Series and Parallel Connections of Resistors

- Elements in series share the same *physical** current
 - Elements in parallel share the same *physical** voltage
- * *Physical* as opposed to *numerical*; e.g., two elements having the same numerical current are not necessarily in series, etc.



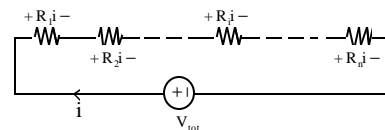
Two elements in series



Two elements in parallel

3.1 Series and Parallel Connections of Resistors

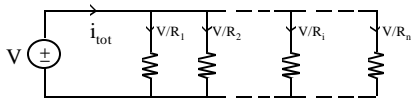
- Resistors in series add: $R_{tot} = R_1 + R_2 + \dots + R_n$



$$\text{KVL: } V_{tot} = \sum_{j=1}^{j=n} R_j i = i \sum_{j=1}^{j=n} R_j = R_{tot} i$$

3.1 Series and Parallel Connections of Resistors

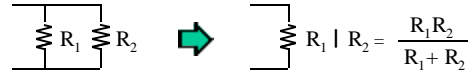
- Resistors in parallel add reciprocally:
 $R_{\text{tot}}^{-1} = R_1^{-1} + R_2^{-1} + \dots + R_n^{-1}$
- And conductances in parallel add directly:
 $G_{\text{tot}} = G_1 + G_2 + \dots + G_n$ (See text p. 60)



$$\text{KCL: } i_{\text{tot}} = \sum_{j=1}^n V/R_j = V \sum_{j=1}^n R_j^{-1} = V R_{\text{tot}}^{-1}$$

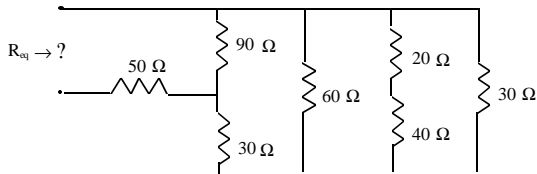
3.1 Series and Parallel Connections of Resistors

- Special case: Two Resistors in parallel:
 $R_1 \parallel R_2 = (R_1 R_2) / (R_1 + R_2)$
- N.B.: Product-over-sum rule and notation (see text p. 61)—memorize!



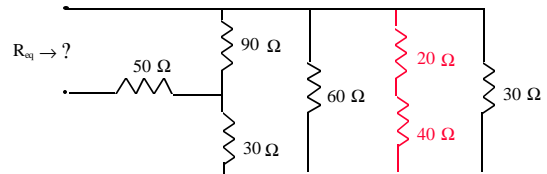
3.1 Series and Parallel Resistors: Example 3-1

Example 3-1: Calculate R_{eq}



3.1 Series and Parallel Resistors: Example 3-1

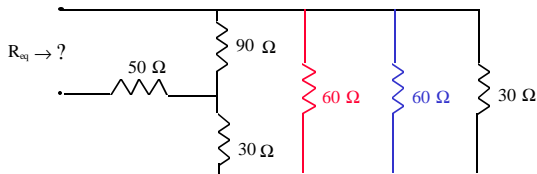
Example 3-1: Calculate R_{eq}



Step 1: $20 \Omega + 40 \Omega = 60 \Omega$ (two series resistors)

3.1 Series and Parallel Resistors: Example 3-1

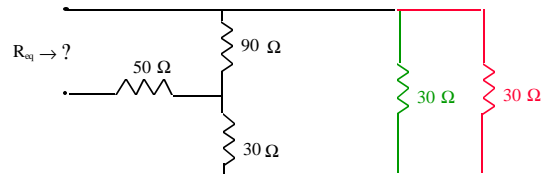
Example 3-1: Calculate R_{eq}



Step 2: $60 \Omega \parallel 60 \Omega = 30 \Omega$ (two parallel resistors)

3.1 Series and Parallel Resistors: Example 3-1

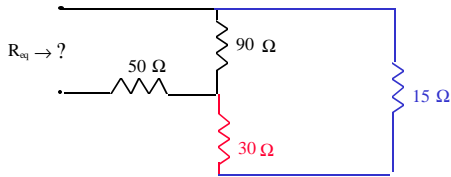
Example 3-1: Calculate R_{eq}



Step 3: $30 \Omega \parallel 30 \Omega = 15 \Omega$ (two parallel resistors)

3.1 Series and Parallel Resistors: Example 3-1

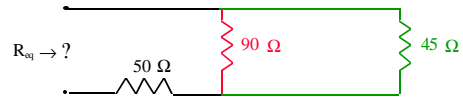
Example 3-1: Calculate R_{eq}



Step 4: $30\ \Omega + 15\ \Omega = 45\ \Omega$ (two series resistors)

3.1 Series and Parallel Resistors: Example 3-1

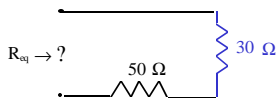
Example 3-1: Calculate R_{eq}



Step 5: $90\ \Omega \parallel 45\ \Omega = 30\ \Omega$ (two parallel resistors)

3.1 Series and Parallel Resistors: Example 3-1

Example 3-1: Calculate R_{eq}



Step 6: $50\ \Omega + 30\ \Omega = 80\ \Omega$ (two series resistors)

3.1 Series and Parallel Resistors: Example 3-1

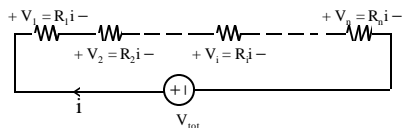
Example 3-1: Calculate R_{eq}



Step 7: Ergo, $R_{eq} = 80\ \Omega$

3.2 Voltage and Current division

- Voltage division: Series resistor voltages divide in proportion to resistances



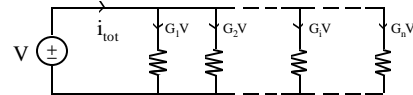
$$\text{KVL: } V_{tot} = R_{tot} i = \left(\sum_{j=1}^n R_j \right) i \quad (\text{I})$$

$$\text{Ohm's Law: } V_i = R_i i \quad (\text{II})$$

$$(\text{II}) \div (\text{I}) \text{ yields: } \frac{V_i}{V_{tot}} = \frac{R_i}{R_{tot}} \quad \text{Memorize!}$$

3.2 Voltage and Current division

- Current division: Parallel resistor currents divide in proportion to conductances



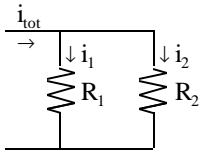
$$\text{KCL: } i_{tot} = G_{tot} V = \left(\sum_{j=1}^n G_j \right) V \quad (\text{I})$$

$$\text{Ohm's Law: } i_i = G_i V \quad (\text{II})$$

$$(\text{II}) \div (\text{I}) \text{ yields: } \frac{i_i}{i_{tot}} = \frac{G_i}{G_{tot}} \quad \text{Memorize!}$$

3.2 Voltage and Current division

- Special case: Two Resistors in parallel:
 $i_1/i_{\text{tot}} = R_2/(R_1 + R_2)$, etc. (see below)
- N.B.: “Other” resistor over sum of resistors (see text p. 68)—memorize!



$$\frac{i_1}{i_{\text{tot}}} = \frac{R_2}{R_1 + R_2}$$

$$\frac{i_2}{i_{\text{tot}}} = \frac{R_1}{R_1 + R_2}$$

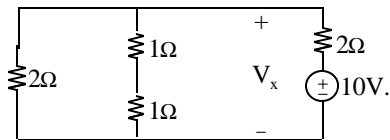
Memorize!

Circuit Analysis Tool kit: Recapitulation

- Single-loop circuit analysis
- Single-node-pair circuit analysis
- Source transformations
- Series-parallel resistance combinations
- Voltage division
- Current division

Example 3-2

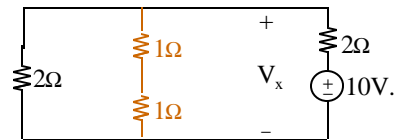
Find V_x



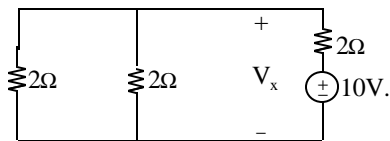
N.B.: See text Problem 3.9, p. 97.

Example 3-2 cont.

Step 1: $1\Omega + 1\Omega = 2\Omega$

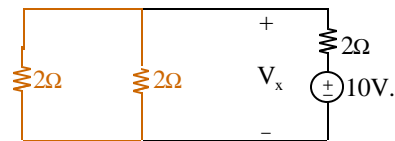


Example 3-2 cont.

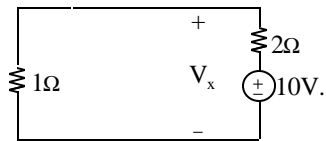


Example 3-2 cont.

Step 2: $2\Omega \parallel 2\Omega = 1\Omega$

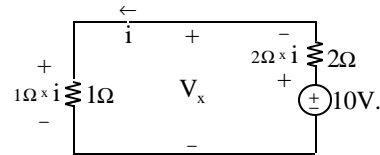


Example 3-2 cont.



Example 3-2 cont.

Step 3: Single-loop circuit
 KVL: $10 \text{ V} - 2\Omega \times i - 1\Omega \times i = 0 \text{ V}$.
 Which has solution $i = 10/3 \text{ A}$.

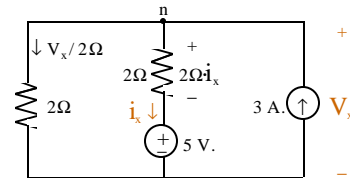


So what's V_x ?

3.3 Superposition

- *Superposition* is the defining (inherent) property of linear systems
- Ergo, *linearity* and *superposition* are synonymous
- Electric circuits are electrical systems
- The behavior of all voltages and currents in electric circuits consisting of constant valued resistors and (independent) voltage and/or current sources is governed by *linear algebraic equations* in these voltages and currents; e.g., consider ...

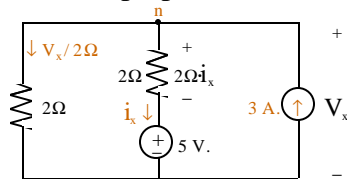
3.3 Superposition cont.



N.B.: See text Problem 3.23, p. 99.

Find V_x and i_x

3.3 Superposition cont.



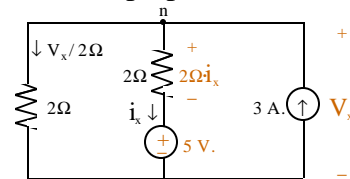
N.B.: See text Problem 3.23, p. 99.

KCL at n

$$V_x/2\Omega + i_x - 3 \text{ A} = 0 \text{ A}$$

(Which is linear in V_x and i_x)

3.3 Superposition cont.



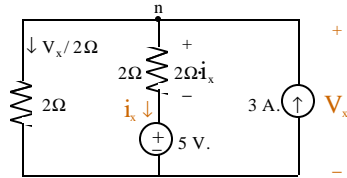
N.B.: See text Problem 3.23, p. 99.

KVL (right mesh)

$$5 \text{ V} + 2\Omega \cdot i_x - V_x = 0 \text{ V}$$

(Also linear in V_x and i_x)

3.3 Superposition cont.



N.B.: See text Problem 3.23, p. 99.

$$V_x / 2\Omega + i_x - 3 \text{ A.} = 0 \text{ A.}$$

$$5 \text{ V.} + 2\Omega \cdot i_x - V_x = 0 \text{ V.}$$

Have solution

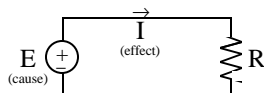
$$V_x = 5.5 \text{ V. and } i_x = 0.25 \text{ A.}$$

3.3 Superposition cont.

- What is the definition of the *Superposition* property?
- *If* effect E_1 results from cause C_1
- *And if* effect E_2 results from cause C_2
- *And if* effect $K \cdot E_2$ results from cause $K \cdot C_2$ (where K is a constant)
- *Then* cause $(C_1 + K \cdot C_2)$ results in effect $(E_1 + K \cdot E_2)$
- And the cause-effect relationship (system) possessing the above *superposition* property is said to be *linear*

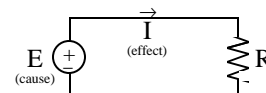
3.3 Superposition cont.

- Are the aforementioned electric circuits linear systems?
- Yes! Consider the one-variable case below where there is one independent voltage source (the cause) and one dependent current variable (the effect)
- Then the cause-effect relationship is mathematical and manifests itself as the linear algebraic equation $I = E/R$ (Ohm's Law) in the dependent variable I



3.3 Superposition cont.

- Then if $E = E_1$, $I = I_1 = E_1/R$ and ...
- And if $E = E_2$, $I = I_2 = E_2/R$ and ...
- And if $E = K \cdot E_2$, $I = K \cdot E_2/R = K \cdot I_2$
- So that when $E = (E_1 + K \cdot E_2)$
- $I = (E_1 + K \cdot E_2)/R = E_1/R + K \cdot E_2/R = I_1 + K \cdot I_2$
- Ergo, superposition applies!



3.3 Superposition cont.

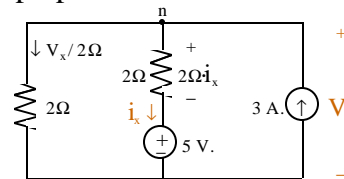
What's the practical use of this property; i.e., what's its application?

One-source-at-a-time superposition!

Which works because, in a linear system, partial effects caused by partial causes can be added to produce the total effect resulting from the sum-total of the partial causes

The key to the method's success lies in partitioning a given problem into single-source sub-problems (which are relatively easy to solve) and then applying superposition to the sub-problems' solutions—by just adding them up!

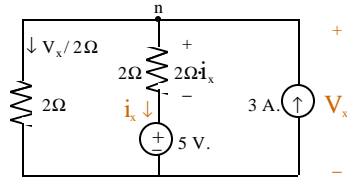
3.3 Superposition cont. —Example 3-3



N.B.: See text Problem 3.23, p. 99.

Find V_x and i_x using *one-source-at-a-time superposition*

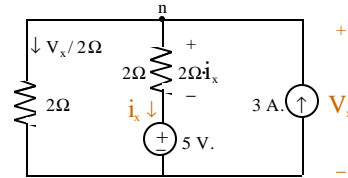
3.3 Superposition cont.—Example 3-3 cont.



N.B.: See text Problem 3.23, p. 99.

Step 1: Calculate the components of V_x and i_x that are caused by the 5 V. voltage source *only*. This begs the question “how is the influence of the 3 A. current source to be withdrawn from consideration?”

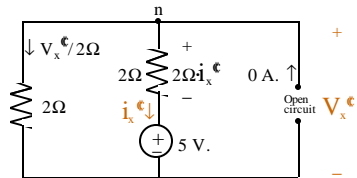
3.3 Superposition cont.—Example 3-3 cont.



N.B.: See text Problem 3.23, p. 99.

Step 1 (cont.): The answer is to replace it with a zero (no) Ampere current source (i.e., an open circuit)—no current, no influence!

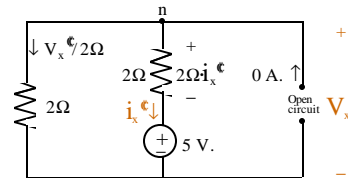
3.3 Superposition cont.—Example 3-3 cont.



N.B.: See text Problem 3.23, p. 99.

Step 1 (cont.): N.B.: The *partial* answers (caused by the 5 V. voltage source only) have been flagged with primes.

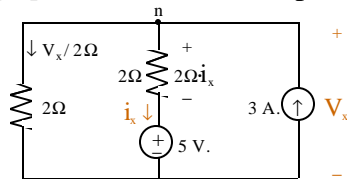
3.3 Superposition cont.—Example 3-3 cont.



N.B.: See text Problem 3.23, p. 99.

Step 1 (cont.): What's left is just a one-loop circuit having (by Ohm's Law) a counterclockwise current of $V_x' / 2\Omega = 5 \text{ V.} / (2\Omega + 2\Omega) = 1.25 \text{ A.} \therefore V_x' = 2.5 \text{ V.}$ and KCL at node n yields $i_x' = -1.25 \text{ A.}$

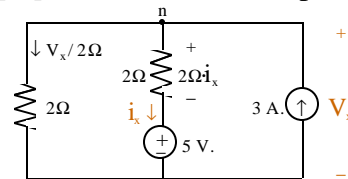
3.3 Superposition cont.—Example 3-3 cont.



N.B.: See text Problem 3.23, p. 99.

Step 2: Calculate the components of V_x and i_x that are caused by the 3 A. current source *only*. This begs the question “how is the influence of the 5 V. voltage source to be withdrawn from consideration?”

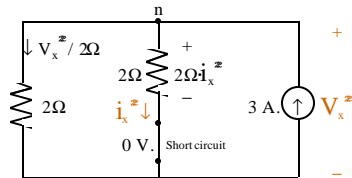
3.3 Superposition cont.—Example 3-3 cont.



N.B.: See text Problem 3.23, p. 99.

Step 2 (cont.): The answer is to replace it with a zero (no) Volt voltage source (i.e., a short circuit)—no voltage, no influence!

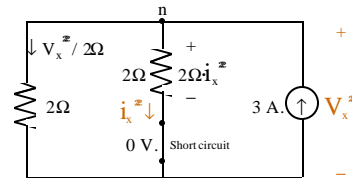
3.3 Superposition cont.—Example 3-3 cont.



N.B.: See text Problem 3.23, p. 99.

Step 2 (cont.): N.B.: The *partial* answers (caused by the 3 A. current source only) have been flagged with double primes.

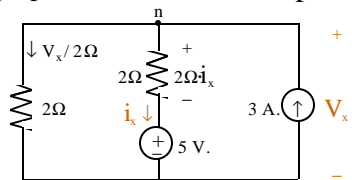
3.3 Superposition cont.—Example 3-3 cont.



N.B.: See text Problem 3.23, p. 99.

Step 2 (cont.): What's left is just a two-(equal) resistor current divider for which $i_x^z = [2\Omega / (2\Omega + 2\Omega)] \cdot 3 \text{ A.} = 1.5 \text{ A.}$ so that $V_x^z = 2\Omega \cdot i_x^z = 2\Omega \cdot 1.5 \text{ A.} = 3 \text{ V.}$

3.3 Superposition cont.—Example 3-3 cont.



N.B.: See text Problem 3.23, p. 99.

Step 3: Calculate each answer by summing its respective components; i.e., $i_x = i_x' + i_x'' = -1.25\text{A.} + 1.5\text{A.} = 0.25 \text{ A.}$ and: $V_x = V_x' + V_x'' = 2.50\text{V.} + 3.0\text{V.} = 5.50 \text{ V.}$

3.3 Superposition cont.

Does superposition work for power?

No! If it did (it *doesn't*), the power absorbed by the 2Ω resistor (the one through which i_x flows) would be $2\Omega(i_x')^2 + 2\Omega(i_x'')^2 = 2\Omega(-1.25\text{A.})^2 + 2\Omega(1.5\text{A.})^2 = 7.625 \text{ W.}$

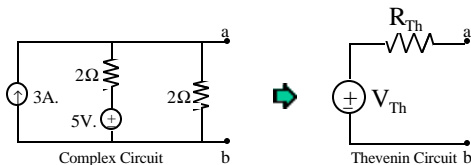
However, the power actually is $2\Omega(i_x)^2 = 2\Omega(0.25\text{A.})^2 = 0.125 \text{ W.}$

Why didn't superposition work for power?

Because $(i_x)^2 = (i_x' + i_x'')^2 = (i_x')^2 + 2i_x'i_x'' + (i_x'')^2 \neq (i_x')^2 + (i_x'')^2$ (i.e., the quadratic's cross-product term is missing)

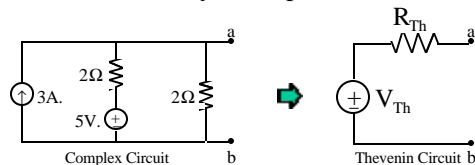
3.4 Thevenin and Norton Equivalent Circuits

- The basic idea is to replace a relatively complex (linear) circuit with a simple *single-loop circuit* having a single voltage source and a single resistor—which is called the complex circuit's *Thevenin Equivalent Circuit*



3.4 Thevenin and Norton Equivalent Circuits

- What's needed are rules for how to calculate V_{Th} and R_{Th}
- Note that all of the numerical data is in the left (complex) circuit whereas the right (Thevenin) circuit is entirely conceptual

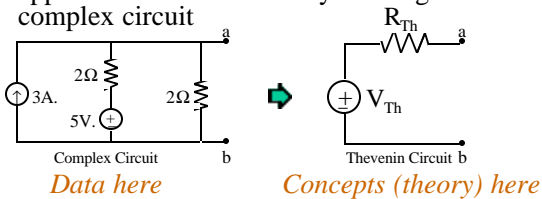


Data here

Concepts (theory) here

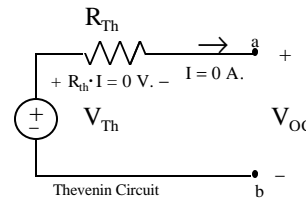
3.4 Thevenin and Norton Equivalent Circuits

- This suggests that the rules for how to calculate V_{Th} and R_{Th} should be derivable from the Thevenin (theory) circuit and ...
- Once derived, these rules are then always applied to the data—namely the original complex circuit



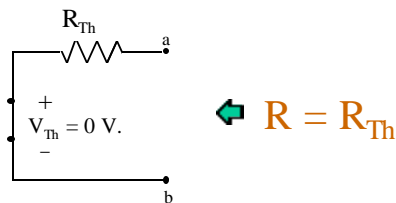
3.4 Thevenin Circuit Element Rules

- KVL applied to the Thevenin circuit *with terminals a-b open* (so $I = 0$ A.) yields:
- $V_{Th} - 0 \text{ V.} - V_{OC} = 0 \text{ V.} \quad \therefore$
- $V_{Th} = V_{OC}$ (Thevenin voltage = Open circuit voltage)



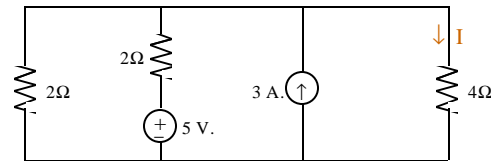
3.4 Thevenin Circuit Element Rules cont.

- R_{Th} is the resistance of the circuit when all independent sources of energy are removed from consideration (all voltage sources shorted, all current sources opened)



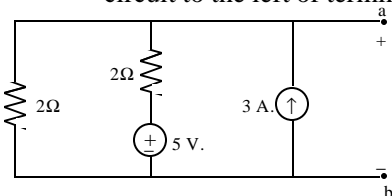
3.4 Thevenin & Norton Equiv. Circuits cont.

Example 3-4 Find I using Thevenin's Theorem



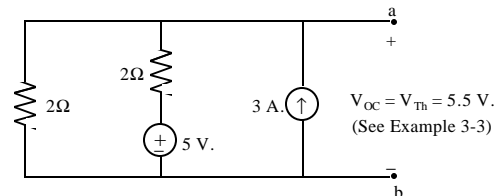
3.4 Example 3-4 cont.

Step 1: Get the Thevenin Equiv. of the circuit to the left of terminals a-b



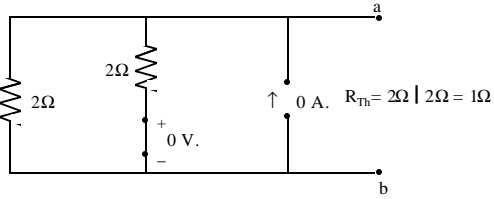
3.4 Example 3-4 cont.

Step 1a: Open circuit voltage calculation



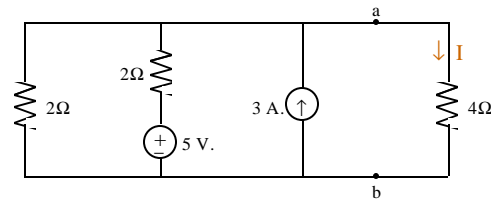
3.4 Example 3-4 cont.

Step 1b: Determination of R_{Th}



3.4 Example 3-4 cont.

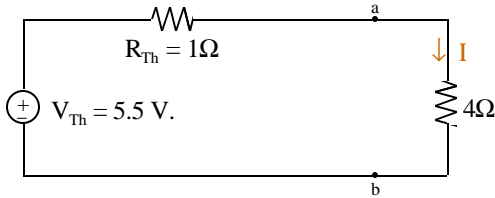
Ergo, finding I using Thevenin's Theorem becomes



3.4 Example 3-4 cont.

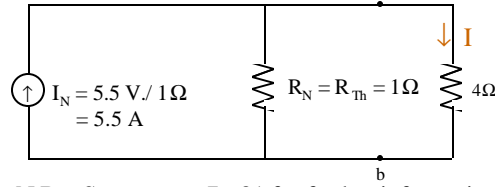
$$I = 5.5 \text{ V.} / (1 + 4) \Omega = 1.1 \text{ A.}$$

(Ohm's Law)



3.4 Example 3-4 cont.

Using source conversions, the Norton solution is: $I = [1\Omega / (1 + 4)\Omega] \times 5.5 \text{ A.} = 1.1 \text{ A.}$ (Current \div)



N.B.: See text pp. 76-81 for further information regarding Norton Equivalent circuits

3.5 Node & Mesh Analysis

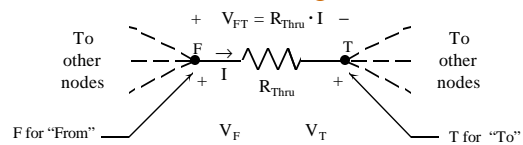
Node voltage analysis is just *organized* KCL(s)

Likewise, mesh current analysis is just *organized* KVL(s)

First consider node voltage analysis

But before that, consider the following useful rule

From-to-through Rule



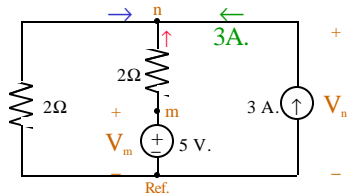
Ref.
(Reference node from which all other voltages are measured)

KVL: $V_F - V_{FT} - V_T = 0 \therefore V_{FT} = V_F - V_T = R_{Thru} \cdot I$ (Ω 's Law)

$$I = \frac{V_{From} - V_{To}}{R_{Thru}} \leftarrow \text{Memorize this formula!}$$

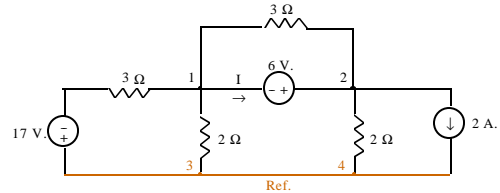
3.5 Node Voltage Analysis: Example 3-5

There are three nodes (*m*, *n* and the Ref. node)
 V_m is known to be 5 V. (by inspection or by KVL)
 Write KCLs at nodes where the voltage is *unknown*
 KCL at node *n*: $(0V - V_n)/2\Omega + (5V - V_n)/2\Omega + 3A = 0$ A. —which has solution $V_n = 5.5$ V.



3.5 Node Voltage Analysis: Example 3-6

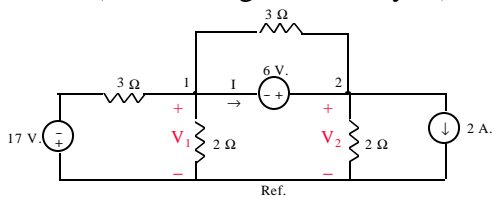
Find *I* using nodal analysis



The first step is to (arbitrarily) establish the "bottom" (physical nodes 3 and 4) of the circuit as the (electrical) reference node (Ref.)

Example 3-6 cont.

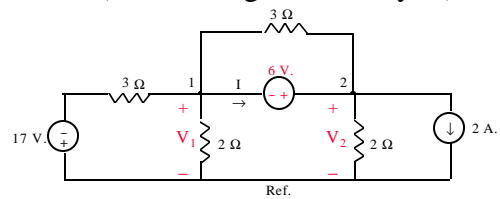
(Find *I* using nodal analysis)



The node voltages V_1 and V_2 are with respect to the reference (bottom) node as shown

Example 3-6 cont.

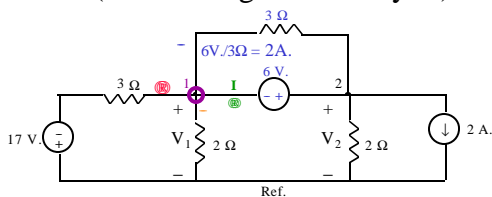
(Find *I* using nodal analysis)



KVL: $V_1 + 6V - V_2 = 0V$. $\therefore V_2 = V_1 + 6$ (A.)

Example 3-6 cont.

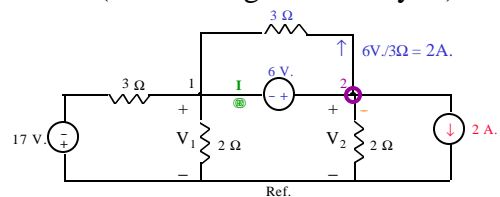
(Find *I* using nodal analysis)



KCL at Node 1:
 $[(-17V) - V_1]/3\Omega + 2A - I - V_1/2\Omega = 0$ A. (B.)

Example 3-6 cont.

(Find *I* using nodal analysis)



KCL at Node 2:
 $I - 2A - 2A - V_2/2\Omega = 0$ A. (C.)

Example 3-6 cont. (Find I using nodal analysis)

Equations (A.), (B.) and (C.) have solution:
 $V_1 = -8 \text{ V.}, V_2 = -2 \text{ V.}$ and $I = 3 \text{ A.}$
 Ergo, $I = 3 \text{ A.}$

8:44 PM Ohio University's Russ College of Engineering & Technology 67

3.5 Mesh Current Analysis: Example 3-7

There are two (left & right) meshes ("window panes")
 I_2 is known to be -3 A. (by inspection or by KCL)
 Write KVLs around meshes whose mesh currents are *unknown*
 KVL (left mesh): $-2\Omega I_1 - 2\Omega(I_1 - I_2) - 5 \text{ V.} = 0 \text{ V.}$
 which given $I_2 = -3 \text{ A.}$ has solution $I_1 = -2.75 \text{ A.}$

8:44 PM Ohio University's Russ College of Engineering & Technology 68

3.5 Mesh Current Analysis: Example 3-8 Find I using mesh analysis

The first step is to (arbitrarily) establish the mesh currents I_1, I_2, I_3 and I_4 as shown

8:44 PM Ohio University's Russ College of Engineering & Technology 69

Example 3-8 cont. (Find I using mesh analysis)

Next, observe that $I_3 = 2 \text{ A.}$ and $I_4 = -6\text{V}/3\Omega = -2 \text{ A.}$
 and alter the schematic accordingly (see next slide)

8:44 PM Ohio University's Russ College of Engineering & Technology 70

Example 3-8 cont. (Find I using mesh analysis)

Next, place *voltage drops* adjacent to the resistors as shown—note the use of the passive sign convention in assigning each voltage polarity!

8:44 PM Ohio University's Russ College of Engineering & Technology 71

Example 3-8 cont. (Find I using mesh analysis)

Next, write KVLs around meshes whose mesh currents are *not* known

8:44 PM Ohio University's Russ College of Engineering & Technology 72

Example 3-8 cont.
(Find I using mesh analysis)

Mesh KVLs:

$$-17 \text{ V.} - 3\Omega \times I_1 - 2\Omega \times (I_1 - I_2) = 0 \text{ V.} \quad (\text{A.})$$

$$2\Omega \times (I_1 - I_2) + 6 \text{ V.} - 2\Omega \times (I_2 - 2) = 0 \text{ V.} \quad (\text{B.})$$

8:44 PM Ohio University's Russ College of Engineering & Technology 73

Example 3-8 cont.
(Find I using mesh analysis)

Equations (A.) and (B.) have solution $I_1 = -3 \text{ A.}$ and $I_2 = 1 \text{ A.}$ so given $I_4 = -2 \text{ A.}$, it follows that $I = I_2 - I_4 = 1 \text{ A.} - (-2 \text{ A.}) = 3 \text{ A.} \therefore I = 3 \text{ A.}$

8:44 PM Ohio University's Russ College of Engineering & Technology 74

3.6 Maximum Power Transfer

To extract maximum power from a Thevenin circuit, load it with a resistance equal to R_{Th} — see text pp. 95-96 for (calculus) proof

It follows then that to extract maximum power from *any* (linear) circuit, load it with its Thevenin resistance R_{Th} with respect to the extraction point

8:44 PM Ohio University's Russ College of Engineering & Technology 75

3.6 Maximum Power Transfer: Example 3-9

What's the maximum power that can be extracted from terminals a-b?

8:44 PM Ohio University's Russ College of Engineering & Technology 76

3.6 Maximum Power Transfer: Example 3-9 cont.

The circuit's Thevenin equivalent (found in Example 3-4) loaded with R_{Th} at terminals a-b yields: $I = 5.5 \text{ V.} / (1 + 1)\Omega = 2.75 \text{ A.}$ so the (maximum) load power is: $P_{max} = I^2 R = (2.75 \text{ A.})^2 \cdot 1 \Omega = 7.5625 \text{ W.}$

8:44 PM Ohio University's Russ College of Engineering & Technology 77

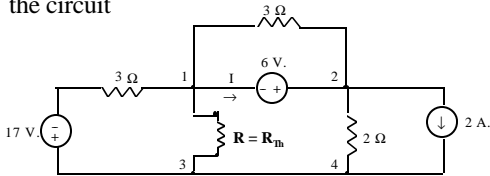
3.6 Maximum Power Transfer: Example 3-10

Determine the value of R in the circuit which will draw maximum power and calculate the corresponding maximum power.

8:44 PM Ohio University's Russ College of Engineering & Technology 78

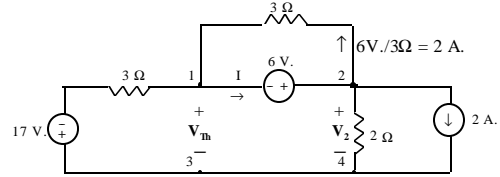
Example 3-10 cont.

Solution strategy: Determine the Thevenin circuit with respect to terminals 1 & 3 — then $R = R_{Th}$ will draw maximum power from the remainder of the circuit



Example 3-10 cont.

First find V_{Th} = open-circuit voltage across terminals 1 & 3



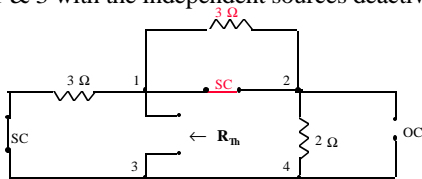
KCL at Node 1: $[(-17V.) - V_{Th}]/3\Omega + 2A. - I = 0$ A. (A.)

KCL at Node 2: $I - 2A. - V_2/2\Omega - 2A. = 0$ A. (B.)

KVL: $V_{Th} + 6V. - V_2 = 0$ V. (C.)
 (A.), (B.) and (C.) have solution $V_{Th} = -12.8$ V.

Example 3-10 cont.

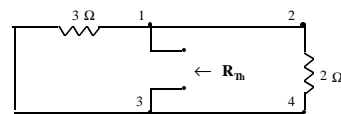
R_{Th} = Resistance across (open-circuited) terminals 1 & 3 with the independent sources deactivated



The parallel combination of the $0\ \Omega$ SC and the $3\ \Omega$ resistor is $0\ \Omega$ (another SC) so the circuit becomes (next slide) ...

Example 3-10 cont.

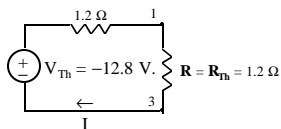
R_{Th} = Resistance across (open-circuited) terminals 1 & 3 with the independent sources deactivated



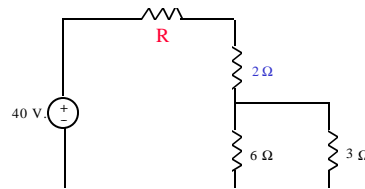
$R_{Th} = 3\ \Omega \parallel 2\ \Omega = 1.2\ \Omega$

Example 3-10 cont.

The circuit's Thevenin equivalent loaded with $R = R_{Th}$ draws a current of:
 $I = V_{Th}/(R_{Th} + R) = (-12.8\ V.)/(1.2\ \Omega + 1.2\ \Omega) = -5\frac{1}{3}A.$
 and the corresponding maximum power is
 $P_{max.} = I^2R = (-5\frac{1}{3}A.)^2 \times 1.2\ \Omega = 34\frac{2}{15}\ W. \approx 34.13\ W.$



3.6 Maximum Power Transfer: Example 3-11



Calculate the value of resistance (in Ω) of the resistor R which maximizes the power absorbed by the $2\ \Omega$ resistor.

Example 3-11 cont.

$P_{2\Omega}$ is maximized when $I = 40 \text{ V.} / (R + 2 \Omega + 6 \Omega \parallel 3 \Omega)$ is maximized—which occurs when $R = 0 \text{ W}$

Ergo, for $R = 0 \Omega$, $I = 40 \text{ V.} / 4 \Omega = 10 \text{ A.}$ so that

$P_{2\Omega, \text{max.}} = 2 \Omega \times I^2 = 2 \Omega \times (10 \text{ A.})^2 = 200 \text{ W.}$

8:44 PM Ohio University's Russ College of Engineering & Technology 85

Example 3-11 cont.

What is achieved if $R = 2 \Omega + 6 \Omega \parallel 3 \Omega = 4 \Omega$?

P_R is maximized—but the goal is to maximize $P_{2\Omega}$ (not P_R)

N.B.: If $R = 4 \Omega$, $I = 5 \text{ A.} \therefore P_{2\Omega} = 2 \Omega (5 \text{ A.})^2 = 50 \text{ W.} < 200 \text{ W.} = P_{2\Omega, \text{max.}}$

Can maximum power transfer theorem impedance matching be used to solve this problem?

Yes! (See next slide)

8:44 PM Ohio University's Russ College of Engineering & Technology 86

Example 3-11 cont.

What's required for maximum power transfer from the Thevenin circuit to the 2Ω load?

$R_{\text{Th}} = R + 6 \Omega \parallel 3 \Omega = 2 \Omega = R_{\text{load}}$ which yields:

$R = 0 \Omega$

If the 6Ω resistor is removed from the circuit, what value of R maximizes the 2Ω resistor's power?

8:44 PM Ohio University's Russ College of Engineering & Technology 87

We welcome your questions with Enthusiasm!!

Brian Manhire, Ph.D.
Professor of Electrical Engineering
OHIO UNIVERSITY

School of Electrical Engineering & Computer Science
Stocker Center
Athens OH 45701-2270
740-593-0179 phone
740-593-0037 fax
bmanhire@ohio.edu

School of Electrical Engineering and Computer Science

Ohio University

Russ College of Engineering & Technology